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## ENERGY AND EXERGY DIAGNOSTICS OF AN INDUSTRIAL ANNULAR SHAFT LIMEKILN WORKING WITH PRODUCER GAS AS RENEWABLE BIOFUEL

### Article Highlights

- Performance results for a limekiln operating with renewable biofuel were presented
- The new results exposed come from energy and exergy diagnostics of the limekiln
- Energy and exergy efficiencies of the limekiln were 54.6 and 42.2%, respectively
- Energy and exergy global efficiencies of the calcination process were 42.0 and 23.6%, respectively
- Results showed that producer gas as renewable biofuel can be competitive

### Abstract

*Quicklime, a globally significant commodity used in various industrial applications, is produced in limekilns requiring substantial energy, traditionally, from fossil fuels. However, due to escalating emission constraints and depletion of fossil fuel deposits, the quicklime industry explores alternative fuels, like biomass. The literature lacks feasibility diagnostic studies on limekilns using alternative biomass fuels. Thus, this article aims to conduct energy and exergy diagnostics on an industrial limekiln using producer gas derived from eucalyptus wood as a renewable biofuel. Employing industrial data and thermodynamics principles, the equipment was characterized, and results were compared with literature findings for similar limekilns using fossil fuels. The Specific Energy Consumption (SEN) for the producer gas-operated limekiln was 4.8 GJ/t<sub>quicklime</sub>, with energy ( $\eta_{en}$ ) and exergy ( $\eta_{ex}$ ) efficiencies of 54.6% and 42.2%. Overall energy ( $\eta_{en-overall}$ ) and exergy ( $\eta_{ex-overall}$ ) efficiencies were 42.0% and 23.6%, respectively, lower than literature values. SEN<sub>overall</sub> was 7.6 GJ/t<sub>quicklime</sub>, higher than the literature results. Identified enhancements for both renewable and fossil fuel-powered limekilns involve recovering energy and exergy, including heat recovery from exhaust gases, minimizing thermal losses, and optimizing operational variables. These findings offer valuable insights for researchers exploring renewable biofuel adoption, like producer gas derived from eucalyptus wood, as alternatives to conventional fossil fuels in limekilns.*

*Keywords: energy, exergy, limekiln, quicklime, biomass, biofuel.*

Quicklime is a solid substance with CaO<sub>(s)</sub> as its main constituent, and it holds global significance due to its various essential applications as a chemical compo-

und. These applications include its use in mortar and cement production, water treatment, air pollution control, glass manufacturing, whitewashing acidic soils, casting steps, and as a chemical absorbent [1]. Moreover, the literature has explored innovative applications and properties of quicklime, such as its use for adsorbent development [2], novel composite material development [3], and the water transfer mechanism of quicklime-modified centrifugal dewatering clay [4]. Among the top five global quicklime producers in 2019 are China, India, USA,

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Russia, and Brazil. Brazil ranks fifth in this list and produced approximately 8.1 million metric tons of quicklime in 2019 [5].

Limestone, predominantly composed of  $\text{CaCO}_{3(s)}$ , is utilized as the raw material for the manufacture of quicklime. In this process, either horizontal or vertical limekilns are employed, where temperatures around 900–1000 °C, are reached by the limestone, leading to the thermal decomposition of  $\text{CaCO}_{3(s)}$  into  $\text{CaO}_{(s)}$  and  $\text{CO}_{2(g)}$ . The heat necessary for the calcination reaction in limekilns is traditionally generated through the combustion of fossil fuels [6].

The most significant factor influencing quicklime production cost is fuel consumption, which accounts for approximately 50% of the total manufacturing cost [7]. In addition to cost considerations, quicklime production stands out as one of the industrial processes with the highest emissions of  $\text{CO}_{2(g)}$  [8]. Specifically, during limestone calcination, 785 kg of  $\text{CO}_{2(g)}$  are emitted per ton of  $\text{CaCO}_{3(s)}$ , and an additional 200–400 kg of  $\text{CO}_{2(g)}$  are emitted during fuel combustion. This results in a total emission of around 1000–1200 kg of  $\text{CO}_{2(g)}$  per ton of produced quicklime [7]. As the  $\text{CO}_{2(g)}$  produced during  $\text{CaCO}_{3(s)}$  calcination remains constant, the total emitted  $\text{CO}_{2(g)}$  depends primarily on the fuel consumption efficiency within the limekiln. [7].

For these reasons, studies aiming to improve the calcination process have been undertaken by authors from various countries across the globe, such as Australia [9], China [10,11], Germany [12], India [13] and Indonesia [14]. However, for Brazil, the fifth largest quicklime producer in the world, there is a gap in the literature regarding studies involving energy and exergy analyses of limekilns operating with renewable biofuels.

The energy efficiency of limekilns can be defined as the ratio between the thermal energy required for the calcination reaction and the energy released by the fuel. Vertical limekilns exhibit higher efficiency (approximately 65–77%) compared to rotary ones (about 40–52%) [15]. Moreover, the Vertical Regenerative Parallel Flow type shows the highest efficiency (around 80–90%), despite its recent technological maturity [6]. These energy analyses have inherent limitations since they are considered solely the first law of thermodynamics [16].

Therefore, exergy analyses can overcome these limitations by incorporating both the first and second laws of thermodynamics. Thus, exergy analyses contribute significantly to the diagnostics of thermodynamic processes, providing a broader understanding of a process and its sustainability, and being able to identify specific parameters to improve

the equipment performance, such as irreversibility points, exergy losses, and fuel-saving points [16].

There are studies in the literature in which energy and exergy analyses of limekilns operating with traditional fossil fuels were performed [7,16]. However, works addressing energy and exergy analyses of limekilns operating with renewable biofuels, such as the present study, were not found in the literature. The current authors have recently conducted experimental analyses involving energy and exergy assessments of other types of equipment, including compressed air energy storage systems [17], kraft biomass boilers [18], clinker rotary kilns [19], and specific chemical exergy predictions for biological molecules [20].

In thermal energy production, the burning of fossil fuels corresponds to one of the main sources of greenhouse gas emissions, mainly  $\text{CO}_{2(g)}$ , which can lead to climate change. Additionally, the depletion of fossil fuel deposits can also imply limitations in the future regarding their uses as energy sources [21]. However, in this scenario, the limekilns are heavily dependent on the employment of solid fossil fuels, oil, and natural gas to meet the equipment's energy demand. These three fossil fuels together represent an employment share of around 90% of the types of fuels used in limekilns [22]. Of these fossil fuels, natural gas is the option that results in the lowest greenhouse gas emissions. Nevertheless, natural gas has a high cost compared to other fossil fuels employed in limekilns.

For these reasons, the lime sector has sought to use other fuel types that meet the increasing limitations on atmospheric emissions, greenhouse gases, product quality, and reduction of quicklime production costs. Favorably, with the deployment of renewable biomass fuels, these requirements aforementioned can be satisfactorily met, which makes biomass an attractive solution for use as biofuel in limekilns. Despite this, the utilization of biomass still represents a small portion of around 2% of the fuels utilized in limekilns [22].

Given the preceding points, it can be perceived that there is a lack of literature regarding energy and exergy diagnostic studies of limekilns operating with biofuels. It is in this regard that the current work aims to contribute to the scientific community. Hence, the present paper aims to conduct energy and exergy diagnostics of a vertical annular shaft limekiln operating with producer gas as a renewable biofuel. To attain this objective, technical visits were made to a calcination industry in the state of Minas Gerais, Brazil. In this company, it was investigated *in situ* how its calcination process is realized, and the employment of producer gas was verified as a renewable biofuel derived from the gasification of eucalyptus wood used as raw

material. Operational data of the calcination process were collected in the aforementioned industry. The applied methodology employed to undertake the diagnostics of the annular shaft limekiln was based on the first and second laws of thermodynamics and mass, energy, and exergy balances of the equipment. Thus, through the proposed diagnostics, investigations were conducted to assess the energy and exergy efficiencies of the limekiln and the calcination process overall, identify points of exergy loss, analyze potential points for exergy recovery, evaluate destroyed exergy, and examine the energy and exergy content of the equipment flows. The results obtained in this study for the limekiln performing with renewable biofuel were compared with literature results for similar vertical annular shaft limekilns operating with traditional fossil fuels. The Specific Energy Consumption ( $SEN$ ) obtained from the limekiln operating with producer gas was 4.8 GJ per ton of quicklime produced, with energy ( $\eta_{en}$ ) and exergy ( $\eta_{ex}$ ) efficiencies of 54.6% and 42.2%, respectively. The overall energy ( $\eta_{en-overall}$ ) and exergy ( $\eta_{ex-overall}$ ) efficiencies of the calcination process were 42.0% and 23.6%, respectively. The  $SEN_{overall}$  of the calcination process was 7.6 GJ per ton of quicklime produced. It was verified that the usage of producer gas as a biofuel derived from eucalyptus wood is technically feasible, sustainable, and can be a solution to the conventional fossil fuels employed in limekilns. Noteworthy enhancements for both renewable and fossil fuel-powered limekilns encompass the recuperation of energy and exergy. This includes mainly heat recovery from exhaust gases, reduction of thermal losses, and optimization of operational parameters. The performance of the calcination process can be improved through the aforementioned suggestions, leading to potential fuel savings and the subsequent reduction in costs and pollutant gas emissions. In addition to the aforementioned contributions, it is expected that this work can also reduce the lack of energy and exergy diagnostics for limekilns operating in Brazil, the fifth-largest global quicklime producer.

## MATERIAL AND METHODS

In this section, the approach utilized for conducting the present study is presented, concerning the characterization of the calcination process, identification of its temperature measurement points, formulation of assumed hypotheses, descriptions of the collected data, and properties of the constituent species of the system.

### Limekiln characterization

Technical visits were conducted to a calcination

company in Minas Gerais, Brazil, where an on-site examination of a vertical annular shaft limekiln was carried out for its operational characterization.

Fig. 1 depicts the aforementioned annular shaft limekiln, with the control volume (CV) encompassing the equipment in continuous operation. It was considered that the equipment operates in a steady state, with constant inlet and outlet conditions, and without mass accumulation. This assumption is proper and commonly considered by the literature for limekilns similar to the one investigated herein [6,16]. The vertical annular shaft limekiln has a cylindrical shape, height of 22 m, diameter of 3.2 m, and wall thickness of 0.4 m. The inner wall of the limekiln is coated with refractory material.

As shown in Fig. 1, eight mass flows  $i$  ( $m_i$ ) cross the CV, where  $i$  represents the substance contained in the flow and is denoted in the subscript as  $ls$ ,  $lm$ ,  $ls-ub$ ,  $pg$ ,  $a$ ,  $pc$ ,  $CO_2(g)-cr$  e  $sw$ , representing limestone, quicklime, unburned limestone, producer gas, combustion air, combustion products,  $CO_2(g)$  released in limestone calcination, and solid waste, respectively. This same nomenclature was also used throughout the current paper to describe a substance contained in a certain flow.

Therefore, as depicted in Fig. 1, a mass flow of limestone ( $m_{ls}$ ) is introduced at the top of the limekiln, while a mass flow of produced quicklime ( $m_{lm}$ ) exits simultaneously from the bottom. Due to gravity, limestone ( $m_{ls}$ ) moves downward and when it reaches the decarbonization temperature in the Calcination Zone it reacts forming  $CaO(s)$  and  $CO_2(g)$ . At the bottom of the limekiln, a mass flow of unburnt limestone ( $m_{ls-ub}$ ) exits, which consist of limestone that does not undergo calcination. A mass flow of producer gas ( $m_{pg}$ ), the renewable biofuel, is introduced into the Calcining Zone along with a mass flow of combustion air ( $m_a$ ). In the Calcination Zone, the producer gas distribution system is assembled to feed the biofuel ( $m_{pg}$ ) through burners, providing the heat of combustion axially and radially in the combustion chamber. In this same region, the combustion air ( $m_a$ ) is introduced with the assistance of air blowers. In the Cooling Zone, in practice, air is also introduced, which comes into contact with the quicklime in this region, cooling it. As a result, this heated air flows upward in countercurrent with the quicklime bed. This ascending heated air not only aids in biofuel combustion but also preheats the limestone at the top of the limekiln. The cooling air was assumed to be a portion of the combustion air ( $m_a$ ). From the Preheating Zone, with the aid of an exhauster, a single flow is released: the mass flow of combustion products ( $m_{pc}$ ) arising from

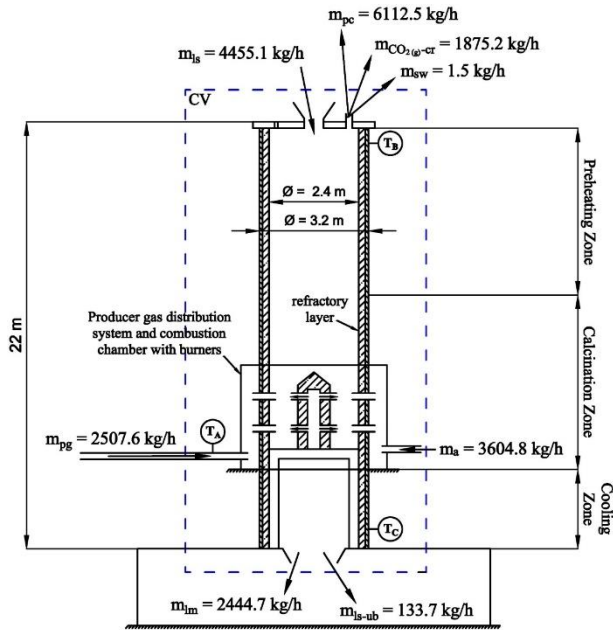


Figure 1. Vertical limekiln.

the burn of the producer gas; the mass flow of  $\text{CO}_2(\text{g})$  ( $m_{\text{CO}_2(\text{g})-\text{cr}}$ ) produced from the limestone calcination, and the mass flow of solid waste ( $m_{\text{sw}}$ ) resulting from limestone attrition.

For operational control of the limekiln, the monitoring of three temperatures is performed at specific points as indicated in Fig. 1: temperature A ( $T_A$ ) is measured at the supply of producer gas; temperature B ( $T_B$ ) is measured at the limekiln top, and temperature C ( $T_C$ ) is controlled at the outlet of the quicklime and unburnt limestone flows at the bottom of the equipment.

## Data collection

Table 1 presents the collected data provided by the company regarding its calcination process during regular working periods, concerning the quantities of component flows, operational temperatures, and chemical composition of limestone and quicklime. Literature data for the chemical composition of producer gas and eucalyptus wood are also provided to complement the system characterization. Additionally, the data for the specific heat polynomials used in the energy and exergy diagnostics are included. To convert masses of chemical species ( $m$ ) to their corresponding moles ( $n$ ), the tabulated molar masses ( $MM$ ) provided by [23] were utilized.

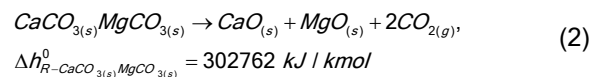
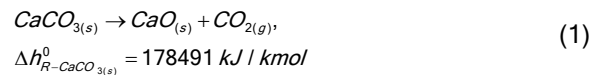
## Temperature characterization

The temperatures ( $T_i$ ) of the mass flows  $i(m_i)$  that cross the limekiln's CV described in Fig. 1 are stated in this subsection. For the mass flow of producer gas ( $m_{\text{pg}}$ ) it

was considered that its temperature ( $T_{\text{pg}}$ ) corresponds to  $T_A = 387.2$  °C. Regarding the mass flows of products of combustion ( $m_{\text{pc}}$ ),  $\text{CO}_2(\text{g})$  from calcination ( $m_{\text{CO}_2(\text{g})-\text{cr}}$ ) and solid wastes ( $m_{\text{sw}}$ ) the temperatures  $T_{\text{pc}}$ ,  $T_{\text{CO}_2(\text{g})-\text{cr}}$  and  $T_{\text{sw}}$  were respectively considered, at  $T_B = 198.2$  °C. For the mass flows of quicklime ( $m_{\text{lm}}$ ) and unburnt limestone ( $m_{\text{ls-ub}}$ ), the temperatures  $T_{\text{lm}}$  and  $T_{\text{ls-ub}}$  were respectively considered, as being  $T_C = 60.0$  °C. For the mass flows of limestone ( $m_{\text{ls}}$ ) and combustion air ( $m_a$ ) the temperatures  $T_{\text{ls}}$  and  $T_a$  were respectively defined, as being at ambient temperature  $T_{\text{env}} = 25.0$  °C.

## Characterization of standard heats of reaction

The chemical species  $\text{CaCO}_3(\text{s})$  and  $\text{CaCO}_3\cdot\text{MgCO}_3(\text{s})$  that constitute the limestone entering the limekiln undergo calcination according to Eqs. (1) and (2), respectively. The standard heats of reaction at 298 K of  $\text{CaCO}_3(\text{s})$  ( $\Delta h_{\text{R}-\text{CaCO}_3(\text{s})}^\circ$ ) and  $\text{CaCO}_3\cdot\text{MgCO}_3(\text{s})$  ( $\Delta h_{\text{R}-\text{CaCO}_3\cdot\text{MgCO}_3(\text{s})}^\circ$ ) were characterized using standard heats of formation ( $\Delta h_{298}^\circ$ ) tabulated and reported by literature [24–27]. The chemical species  $\text{SiO}_2(\text{s})$ ,  $\text{Al}_2\text{O}_3(\text{s})$ , and  $\text{Fe}_2\text{O}_3(\text{s})$  that constitute the limestone are inert.



For the producer gas, its constituent chemical species  $\text{CH}_4(\text{g})$ ,  $\text{CO}(\text{g})$ , and  $\text{H}_2(\text{g})$  undergo combustion according to the chemical reactions expressed by Eqs. (3–5), respectively. The heats of the combustion reaction of  $\text{CH}_4(\text{g})$  ( $\Delta h_{\text{R}-\text{CH}_4(\text{g})}^\circ$ ),  $\text{CO}(\text{g})$  ( $\Delta h_{\text{R}-\text{CO}(\text{g})}^\circ$ ), and  $\text{H}_2(\text{g})$  ( $\Delta h_{\text{R}-\text{H}_2(\text{g})}^\circ$ ) were also characterized by employing the  $\Delta h_{298}^\circ$  tabulated and provided by literature [24–27]. The other chemical species that constitute the producer gas, which are  $\text{CO}_2(\text{g})$ , and  $\text{N}_2(\text{g})$ , do not undergo combustion.

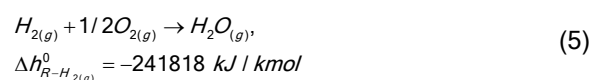
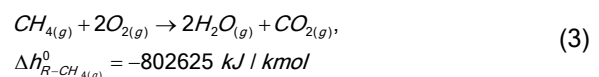


Table 1. Data from the calcination process for the visited company.

COLLECTED DATA							
Flows	Value (kg/h)		Temperature	Value (°C)			
Limestone ( $m_{ls}$ )	4455.1		Temperature A ( $T_A$ )	387.2			
Quicklime ( $m_{lm}$ )	2444.7		Temperature B ( $T_B$ )	198.2			
Unburnt limestone ( $m_{ls-ub}$ )	133.7		Temperature C ( $T_C$ )	60.0			
Solid waste ( $m_{sw}$ )	1.5						
CO <sub>2(g)</sub> from calcination ( $m_{CO_2-cr}$ )	1875.2						
Eucalyptus wood ( $m_{ew}$ )	5147.2						
CHEMICAL COMPOSITION DATA							
Limestone				Quicklime			
Species	Value	Reference	Species	Value	Reference		
CaCO <sub>3(s)</sub>	93.35%wt		CaO <sub>(s)</sub>	95.10%wt			
CaCO <sub>3</sub> ·MgCO <sub>3(s)</sub>	4.94%wt		MgO <sub>(s)</sub>	1.90%wt			
SiO <sub>2(s)</sub>	1.55%wt	This work	SiO <sub>2(s)</sub>	2.73%wt	This work		
Al <sub>2</sub> O <sub>3(s)</sub>	0.09%wt		Al <sub>2</sub> O <sub>3(s)</sub>	0.15%wt			
Fe <sub>2</sub> O <sub>3(s)</sub>	0.07%wt		Fe <sub>2</sub> O <sub>3(s)</sub>	0.12%wt			
Producer gas				Eucalyptus wood			
Species	Value	Reference	Species	Value	Reference		
N <sub>2(g)</sub>	50.00%vol		C	45.19%wt			
CO <sub>(g)</sub>	14.00%vol		O	48.89%wt			
H <sub>2(g)</sub>	9.00%vol	[37]	H	5.82%wt	[38]		
CO <sub>2(g)</sub>	20.00%vol		N	0.10%wt			
CH <sub>4(g)</sub>	7.00%vol		Ash (A)	0.10%wt			
MM <sub>pg</sub>	28.03 kg/kmol	[39]	LHV <sub>ew</sub>	18.27 MJ/kg	[40]		
LHV <sub>pg</sub>	2.94 MJ/m <sup>3</sup>						
SPECIFIC HEAT POLYNOMIAL COEFFICIENTS							
Species	A	B	C	D	E	Validity (K)	Equation
CaCO <sub>3(s)</sub>	12.572	0.002637	0	-312000	-	298-1200	6
CaCO <sub>3</sub> ·MgCO <sub>3(s)</sub>	141.5	0.1359	2175000		-	298-650	7
SiO <sub>2(s)</sub>	4.871	0.005365	0	-100100	-	298-847	6
Al <sub>2</sub> O <sub>3(s)</sub>	102.4290	38.7498	-15.9109	2.6282	-3.0076	298-2327	6
Fe <sub>2</sub> O <sub>3(s)</sub>	11.812	0.009697	0	-197600	-	298-960	6
CaO <sub>(s)</sub>	6.104	0.000443	0	-104700	-	298-2000	6
MgO <sub>(s)</sub>	47.2600	5.6816	-0.8727	0.1043	-1.0540	298-3105	8
CH <sub>4(g)</sub>	1.702	0.009081	-0.000002164	0	-	298-1500	6
CO <sub>(g)</sub>	3.376	0.000557	0	-3100	-	298-2500	6
H <sub>2(g)</sub>	3.249	0.000422	0	8300	-	298-3000	6
CO <sub>2(g)</sub>	5.457	0.001045	0	-115700	-	298-2000	6
O <sub>2(g)</sub>	3.639	0.000506	0	-22700	-	298-2000	6
N <sub>2(g)</sub>	3.28	0.000593	0	4000	-	298-2000	6
H <sub>2</sub> O <sub>(g)</sub>	3.47	0.00145	0	12100	-	298-2000	6

### Characterization of chemical species constituting the mass flows

Each mass flow  $i$  ( $m_i$ ) that crosses the limekiln's CV, is a mixture of solids or gases constituted by chemical species  $j$ . The species  $j$  constituting the mass flows of limestone ( $m_{ls}$ ), quicklime ( $m_{lm}$ ) and producer gas ( $m_{pg}$ ) were mentioned in their chemical compositions presented in Table 1. The mass flow of combustion air is composed of the molar proportion of 21% O<sub>2(g)</sub> and 79% N<sub>2(g)</sub> since the air inserted is atmospheric. The species  $j$  that constitute  $m_{ls}$ , also compose the mass flows of unburnt limestone ( $m_{ls-ub}$ ) and solid waste ( $m_{sw}$ ) arising from limestone friction. The mass flow of combustion products consists of CO<sub>2(g)</sub>, O<sub>2(g)</sub>, N<sub>2(g)</sub> and H<sub>2</sub>O<sub>(g)</sub>, according to the reactions described in Eqs. (3–5) and considering air excess commonly employed in limekilns.

### Specific heat

For the specific heats ( $C_{pj}$ ) of chemical species  $j$

constituents of the mass flows ( $m_i$ ) that cross the limekiln's CV, the characteristic polynomials as a temperature function, characterized by Eqs. (6–8), were considered according to the references indicated [24–26]. The coefficients of these equations for each chemical species are presented in Table 1, as well as their temperature validity ranges and corresponding equations. The mass flow temperatures  $i$  ( $T_i$ ) must be utilized in Kelvin. In Eqs. (7) and (8), the  $C_{pj}$  output unit is kJ/(kmol·K). In Eq. (6), the  $C_{pj}/R$  ratio is used by the reference to make the equation dimensionless, and the  $C_{pj}$  the output unit is the same as the universal gas constant ( $R$ ) employed in this work, which was 8.31446 kJ/(kmol·K).

$$C_{pj} / R \rightarrow A + BT_i + CT_i^2 + DT_i^3 \quad (6) [24]$$

$$C_{pj} \rightarrow A + BT_i - CT_i^{-2}, \text{ kJ} / (\text{kmol} \cdot \text{K}) \quad (7) [25]$$

$$C_{pj} \rightarrow A + Bt_i + Ct_i^2 + Dt_i^3 + Et_i^{-2}, \text{ kJ} / (\text{kmol} \cdot \text{K}) \quad (8) [26]$$

$$t_i = T_i / 1000$$

## MATHEMATICAL DESCRIPTION

The data, characterizations, and considerations previously provided were utilized in the mathematical description described separately in the following. Although the procedure employed is for a vertical annular shaft limekiln operating with producer gas as a renewable biofuel, in general, it can be replicated for other types of renewable biofuels and limekilns.

### Mass Balance

The limekiln's CV was schematically illustrated in Fig. 2a with the mass flows  $i(m_i)$  involved. Limekilns are commonly and properly analyzed in the literature as operating in a steady state, as the equipment works continuously with constant inlet and outlet conditions [6, 16]. So, in Eq. (9), applying the mass conservation principle and considering steady state, it is implied that the sum of input mass flows  $i(m_{in-CV})$  is equivalent to the sum of output mass flows  $i(m_{out-CV})$  in kg/h:

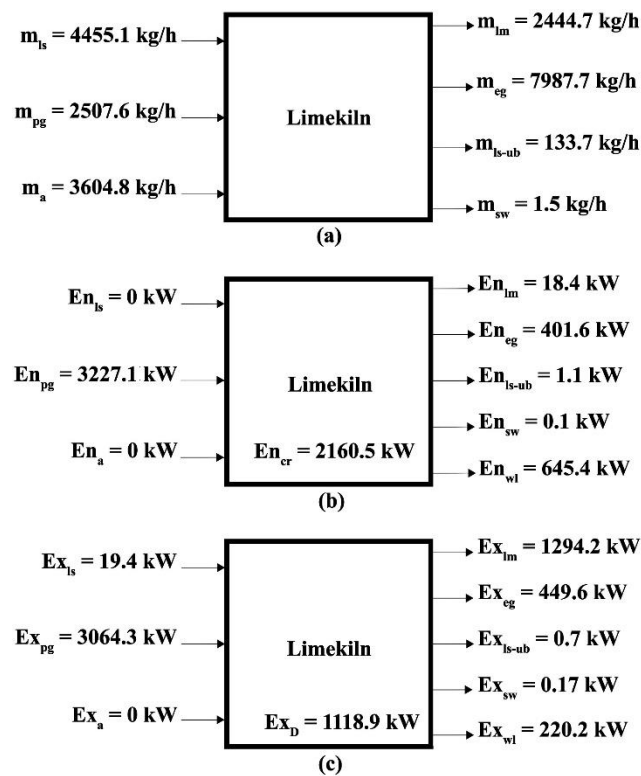


Figure 2. (a) Mass balance; (b) Energy Balance; (c) Exergy balance.

$$\sum m_{in-CV} = \sum m_{out-CV} \quad (9)$$

no mass is accumulated in the CV; therefore, substituting the mass flows ( $m_i$ ) of the CV in Eq. (9) results in:

$$m_{ls} + m_{pg} + m_a = m_{lm} + m_{eg} + m_{ls-ub} + m_{sw} \quad (10)$$

where the mass flows correspond to limestone ( $m_{ls}$ ), producer gas ( $m_{pg}$ ), combustion air ( $m_a$ ), quicklime ( $m_{lm}$ ), exhaust gases ( $m_{eg}$ ), unburnt limestone ( $m_{ls-ub}$ ) and solid waste ( $m_{sw}$ ).

The mass flow of exhaust gases ( $m_{eg}$ ) is characterized by the sum of the mass flows of combustion products ( $m_{pc}$ ) and  $CO_{2(g)}$  generated in calcination ( $m_{CO_{2(g)}-cr}$ ), thus:

$$m_{eg} = m_{pc} + m_{CO_{2(g)}-cr} \quad (11)$$

Each mass flow  $i(m_i)$  in Eq. (10) is a mixture of solids or gases composed by the sum of the masses of constituent chemical species  $j(m_j)$  characterized in the previous chapter, as follows:

$$m_i = \sum_{j=1}^p m_j \quad (12)$$

The evaluation of the combustion air quantity for the producer gas was performed using stoichiometry and considering an excess of air. Thus, initially, based on the combustion reactions of the producer gas characterized by Eqs. (3–5), the stoichiometric number of moles of oxygen ( $n_{O_{2(g)}-ST}$ ) was determined as:

$$n_{O_{2(g)}-ST} = \left( n_{CH_{4(g)}-pg} \cdot 2 + \frac{n_{CO_{(g)}-pg}}{2} + \frac{n_{H_{2(g)}-pg}}{2} \right) \quad (13)$$

in which  $n_{CH_{4(g)}-pg}$ ,  $n_{CO_{(g)}-pg}$  and  $n_{H_{2(g)}-pg}$  are the mole numbers of the species indicated in the subscripts present in the producer gas, whose percentages for each component were provided in Table 1 and can be expressed in terms of the mole number of the producer gas ( $n_{pg}$ ) as follows:

$$n_{CH_{4(g)}-pg} = 0.07n_{pg} \quad (14)$$

$$n_{CO_{(g)}-pg} = 0.14n_{pg} \quad (15)$$

$$n_{H_{2(g)}-pg} = 0.09n_{pg} \quad (16)$$

By substituting Eqs. (14–16) into Eq. (13), the expression for  $n_{O_{2(g)}-ST}$  becomes:

$$n_{O_{2(g)}-ST} = \left( 0.07n_{pg} \cdot 2 + \frac{0.14n_{pg}}{2} + \frac{0.09n_{pg}}{2} \right) \quad (17)$$

And after simplifying,  $n_{O_{2(g)}-ST}$  is equivalent to:

$$n_{O_{2(g)}-ST} = 0.255n_{pg} \quad (18)$$

The air introduced into the limekiln is atmospheric, and it was considered to have a molar composition of 21% O<sub>2(g)</sub> and 79% N<sub>2(g)</sub>. Therefore, taking this composition into account, the number of mols of stoichiometric air ( $n_{a-ST}$ ) was evaluated as follows:

$$n_{O_{a-ST}} = \frac{0.255n_{pg}}{0.21} \quad (19)$$

However, to ensure the complete burning of fuel, it is common to use an air excess. Typical values of excess combustion air employed in limekilns, similar to the one investigated herein, are 5 to 25% [28], 10% [7], and 15 and 32% [16]. The visited company was unable to provide us with the data regarding the quantity of air fed into the limekiln. Thus, based on the characteristics of the limekiln of the industry visited and the literature data aforementioned for analogous limekilns, in this work the excess combustion air was estimated to be 15% of the stoichiometric air. So, the number of moles of air ( $n_a$ ) fed into the limekiln, considering the 15% excess air, was evaluated as follows:

$$n_a = 1.15n_{a-ST} \quad (20)$$

Substituting Eq. (19) into Eq. (20) and simplifying,  $n_a$  becomes:

$$n_a = 1.15 \frac{0.255n_{pg}}{0.21} = 1.397n_{pg} \quad (21)$$

Using the relation  $n = m/MM$ , Eq. (21) becomes as follows:

$$\frac{m_a}{M \cdot M_a} = 1.397 \frac{m_{pg}}{M \cdot M_{pg}} \quad (22)$$

where the molar mass of atmospheric air ( $MM_a$ ) of 28.85 kg/kmol and the molar mass of the producer gas of 28.03 kg/kmol given in Table 1 were employed. Therefore, inputting these  $MM$  values in Eq. (22), it becomes:

$$m_a = 1.438 \cdot m_{pg} \quad (23)$$

### Energy balance

Fig. 2b shows the limekiln's CV with the energy flows  $i$  ( $En_i$ ) involved. In this CV, considering steady state, the sum of input energies  $i$  ( $En_{in-CV}$ ) is equivalent to the sum of output energies  $i$  ( $En_{out-CV}$ ) plus the energy required for calcination ( $En_{cr}$ ), to satisfy the energy conservation principle, as expressed in Eq. (24):

$$\sum En_{in-CV} = \sum En_{out-CV} + En_{cr} \quad (24)$$

and substituting the energy flows ( $En_i$ ) in Eq. (24) results in:

$$En_{ls} + En_{pg} + En_a = En_{lm} + En_{eg} + En_{ls-ub} + E_{sw} + E_{wl} + En_{cr} \quad (25)$$

in which the energy flows in kW correspond to limestone ( $En_{ls}$ ), producer gas ( $En_{pg}$ ), combustion air ( $En_a$ ), quicklime ( $En_{lm}$ ), exhaust gases ( $En_{eg}$ ), calcination ( $En_{cr}$ ), unburnt limestone ( $En_{ls-ub}$ ), solid waste ( $En_{sw}$ ) and wall loss ( $En_{wl}$ ).

The energy flow of exhaust gases ( $En_{eg}$ ) is characterized by the sum of the energy flows of combustion products ( $En_{pc}$ ) and CO<sub>2(g)</sub> generated in calcination ( $En_{CO_2(g)-cr}$ ), as follows:

$$En_{eg} = En_{pc} + En_{CO_2(g)-cr} \quad (26)$$

To determine the energy flows  $i$  ( $En_i$ ) corresponding to  $En_{ls}$ ,  $En_a$ ,  $En_{lm}$ ,  $En_{ls-ub}$ ,  $En_{CO_2(g)-cr}$ ,  $En_{pc}$  and  $En_{sw}$ , in Eq. (27) was used, considering the constituent chemical species  $j$  in each flow. The specific heats ( $Cp_j$ ) of the species and mass flow temperatures ( $T_i$ ) were presented in Table 1. The reference state temperature ( $T_0$ ) considered was 298 K. The species molar flows ( $n_j$ ) was determined through the molar mass conversion mentioned previously.

$$En_i = \sum_{j=1}^n \left( \int_{T_0}^{T_i} Cp_j \cdot dT \right) \cdot n_j \quad (27)$$

The calcination reaction energy ( $En_{cr}$ ) is equivalent to the heats of the reaction of CaCO<sub>3(s)</sub> ( $\Delta h_{R-CaCO_3(s)}$ ) and CaCO<sub>3</sub>·MgCO<sub>3(s)</sub> ( $\Delta h_{R-CaCO_3 \cdot MgCO_3(s)}$ ), defined respectively in Eqs. (1) and (2), multiplied by the molar flows of these chemical species present in the limestone, as follows:

$$En_{cr} = \left( \Delta_{R-CaCO_3(s)}^0 \cdot n_{CaCO_3(s)} \right) + \left( \Delta_{R-CaCO_3(s)MgCO_3(s)}^0 \cdot n_{CaCO_3(s)MgCO_3(s)} \right) \quad (28)$$

Values of thermal energy flow lost through the limekiln walls ( $En_{wl}$ ) are mentioned in the literature as being 4.6 and 9.1% [16], and 9.67 and 14.69% [6] of the available energy. Hence, because of the characteristics of the limekiln investigated herein,  $En_{wl}$  was considered to be 20% of the energy provided by the producer gas ( $En_{pg}$ ), thus:

$$En_{wl} = 0.2En_{pg} \quad (29)$$

Similar ways to estimate  $En_{wl}$  was also performed [7].

The energy flow of producer gas ( $En_{pg}$ ) was calculated through the sum of the heats of combustion of the species  $j$  ( $\Delta h_{R-j}^{\circ}$ ) that undergo combustion plus their integrals of  $Cp_j$  as a temperature function, and each multiplied by the respective molar flows ( $n_j$ ), as follows:

$$\begin{aligned}
 En_{pg} = & \left( \Delta_{R-CH_4(g)}^{\circ} + \int_{660.30}^{298.15} Cp_{CH_4(g)} \cdot dT \right) \cdot n_{CH_4(g)} + \\
 & \left( \Delta_{R-CO(g)}^{\circ} + \int_{660.30}^{298.15} Cp_{CO(g)} \cdot dT \right) \cdot n_{CO(g)} + \\
 & \left( \Delta_{R-H_2(g)}^{\circ} + \int_{660.30}^{298.15} Cp_{H_2(g)} \cdot dT \right) \cdot n_{H_2(g)} + \\
 & \left( \Delta_{R-CO_2(g)}^{\circ} + \int_{660.30}^{298.15} Cp_{CO_2(g)} \cdot dT \right) \cdot n_{CO_2(g)} + \\
 & \left( \Delta_{R-N_2(g)}^{\circ} + \int_{660.30}^{298.15} Cp_{N_2(g)} \cdot dT \right) \cdot n_{N_2(g)}
 \end{aligned} \quad (30)$$

In Eq. (30), values for  $\Delta h_{R-CH_4(g)}^{\circ}$ ,  $\Delta h_{R-CO(g)}^{\circ}$  and  $\Delta h_{R-H_2(g)}^{\circ}$  were given in Eqs. (3–5), respectively; the species  $Cp_j$  polynomials for integral calculation were provided in Table 1; the molar flows of producer gas species ( $n_j$ ) can be converted to species mass flows ( $m_j$ ) utilizing  $MM_j$  values, and then  $m_j$  can be put as a function of the mass flow of producer gas ( $m_{pg}$ ) employing its chemical composition supplied in Table 1. So, by doing this procedure and then simplifying, Eq. (30) can be transformed into an equation of  $En_{pg}$  as a function of  $m_{pg}$ , as follows:

$$En_{pg} = 1.2869m_{pg} \quad (31)$$

The energy flow of combustion products ( $En_{pc}$ ) was determined through the Eq. (27) principle, for its constituent  $j$  species, in this way:

$$\begin{aligned}
 En_{pc} = & \left( \int_{298.0}^{471.4} Cp_{H_2O(g)} \cdot dT \right) \cdot n_{H_2O(g)} + \left( \int_{298.0}^{471.4} Cp_{CO_2(g)} \cdot dT \right) \cdot n_{CO_2(g)} + \\
 & \left( \int_{298.0}^{471.4} Cp_{O_2(g)} \cdot dT \right) \cdot n_{O_2(g)} + \left( \int_{298.0}^{471.4} Cp_{N_2(g)} \cdot dT \right) \cdot n_{N_2(g)}
 \end{aligned} \quad (32)$$

In Eq. (32),  $Cp_j$  polynomials were also given in Table 1; through stoichiometry of the combustion reactions described in Eqs. (3–5), the species molar flows of combustion products can be represented as a function of molar flows of producer gas reacting species and combustion air; and then these reacting species molar flows of producer gas and combustion air can be converted to mass flows  $m_{pg}$  and  $m_a$  employing the chemical compositions given in Table 1, air molar

proportion considered and  $MM$  values. Therefore, by doing this procedure in Eq. (32) and then simplifying it,  $En_{pc}$  can be put in terms of  $m_{pg}$  and  $m_a$ , as follows:

$$En_{pc} = 0.06822m_{pg} + 0.04014m_a \quad (33)$$

### Equation system

A system can be defined by a set of eight equations, Eqs. (10), (11), (23), (25), (26), (29), (31), and (33), having the following eight variables as output data:  $m_{pg}$ ,  $m_a$ ,  $m_{pc}$ ,  $m_{eg}$ ,  $En_{pg}$ ,  $En_{eg}$ ,  $En_{pc}$  e  $En_{wl}$ , and the remaining variables as input data previously calculated. To solve this equation system, the Solver add-in was employed in Excel software with GRG Nonlinear solution method, multiple starting points, and convergence of  $1 \cdot 10^{-10}$ . Overall solutions were found.

With all mass and energy flows determined, it was then possible to calculate the exergy balance variables described in the following section.

### Exergy balance

The limekiln's CV is presented in Fig. 2c with representation of the exergy flows  $i$  ( $Ex_i$ ) involved. Through an exergy balance, and considering a steady state, the sum of input exergy flows  $i$  ( $Ex_{in-CV}$ ) is equivalent to the sum of output exergy flows  $i$  ( $Ex_{out-CV}$ ), plus the destroyed exergy flow ( $Ex_D$ ), thus [16,29]:

$$\sum Ex_{in-CV} = \sum Ex_{out-CV} + Ex_D \quad (34)$$

therefore, replacing the exergy flows results in:

$$Ex_{ls} + Ex_{pg} + Ex_a = Ex_{lm} + Ex_{eg} + Ex_{ls-ub} + Ex_{sw} + Ex_{wl} + Ex_D \quad (35)$$

where the exergy flows in kW correspond to limestone ( $Ex_{ls}$ ), producer gas ( $Ex_{pg}$ ), combustion air ( $Ex_a$ ), quicklime ( $Ex_{lm}$ ), exhaust gases ( $Ex_{eg}$ ), unburnt limestone ( $Ex_{ls-ub}$ ), solid waste ( $Ex_{sw}$ ), wall loss ( $Ex_{wl}$ ) and destroyed exergy ( $Ex_D$ ).

In Eq. (35), each exergy flow  $i$  ( $Ex_i$ ) for solid and gas flows corresponds to the sum of their fractions of physical ( $Ex_{ph,i}$ ) and chemical ( $Ex_{ch,i}$ ) exergies  $i$ , thus:

$$Ex_i = Ex_{ph,i} + Ex_{ch,i} \quad (36)$$

The physical exergy ( $Ex_{ph,i}$ ) for a flow  $i$  of solids or gases was calculated through the sum of physical exergies of constituent chemical species  $j$  of that flow,



as follows [29]:

$$Ex_{p,i} = \sum_{j=1}^p [(h_j - h_0) - T_0(s_j - s_0)] \cdot n_j \quad (37)$$

in which  $h_j$  and  $s_j$  are the specific enthalpy and entropy of the chemical species  $j$  evaluated at the flow conditions,  $h_0$  and  $s_0$  are the specific enthalpy and entropy of the chemical species  $j$  at the dead state,  $n_j$  is the molar flow of the chemical species  $j$ , and  $T_0$  is the temperature at dead state, which was considered 298 K and 101.325 kPa. In Eq. (37), enthalpy and entropy variations were calculated with Eqs. (38) and (39), respectively, considering specific heat varying with temperature [29]:

$$(h_j - h_0) = \int_{T_0}^{T_j} Cp_j dT \quad (38)$$

$$(s_j - s_0) = \int_{T_0}^{T_j} \frac{Cp_j}{T} dT - R \ln \frac{P_i}{P_0} \quad (39)$$

In Eq. (39), the pressure term is assessed solely for gases, and not for liquids and solids. Nevertheless, the system is open and is at reference state pressure ( $P_0$ ), and the pressure of the flows  $i$  ( $P_i$ ) are equal to  $P_0$ . So, the pressure term is negligible for gases since  $P_i = P_0$  [29].

The chemical exergies ( $Ex_{ch,i}$ ) for solid flows  $i$  were determined as follows [30]:

$$Ex_{ch,i} = \sum_{j=1}^p ex_{ch,j} \cdot n_j \quad (40)$$

where the specific chemical exergies ( $ex_{ch,j}$ ) of substances  $j$  are tabulated [31].

To determine chemical exergies ( $Ex_{ch,i}$ ) of flows  $i$  composed of a mixture of gases  $j$ , the following equation was employed [30]:

$$Ex_{ch,i} = \left( \sum_{j=1}^p x_j ex_{ch,j} + RT_0 \sum_{j=1}^p x_j \ln x_j \right) \cdot n_j \quad (41)$$

in which  $x_j$ ,  $R$  and  $n_i$  are, respectively, the mole fraction of chemical species  $j$  in the mixture, universal gas constant, and molar flow of the gas mixture  $i$ .

The wall heat loss exergy flow ( $Ex_{wl}$ ) can be estimated to be 0.09 kW/(kg<sub>quicklime</sub>/h) [16].

### Energy and exergy efficiencies and specific energy consumption

In calcination companies, the energy efficiency of a limekiln ( $\eta_{en}$ ) is conventionally determined by dividing

the energy necessary for calcination ( $En_{cr}$ ) by the product of fuel consumption and the lower calorific value of the fuel [32]. Therefore, considering the producer gas, the energy efficiency of the limekiln was calculated as follows:

$$\eta_{en} = \frac{En_{cr}}{V_{pg} LHV_{pg}} \quad (42)$$

where  $V_{pg}$  and  $LHV_{pg}$  are the volumetric consumption and lower calorific value of the producer gas, respectively.

On the other hand, when considering the gasification of eucalyptus wood into producer gas, the overall energy efficiency ( $\eta_{en-overall}$ ) of the calcination process was assessed based on the energy provided by the eucalyptus wood:

$$\eta_{en-overall} = \frac{En_{cr}}{m_{ew} LHV_{ew}} \quad (43)$$

in which  $m_{ew}$  and  $LHV_{ew}$  are the mass flow and lower calorific value of the eucalyptus wood, respectively.

The exergy efficiency of the limekiln ( $\eta_{ex}$ ) was determined as follows [16]:

$$\eta_{ex} = \frac{Ex_{ch,lm}}{Ex_{pg}} \quad (44)$$

where  $Ex_{ch,lm}$  is the chemical exergy of the quicklime and  $Ex_{pg}$  is the exergy of producer gas consumed by the limekiln.

Similar to the approach employed for the overall energy efficiency, the overall exergy efficiency ( $\eta_{ex-overall}$ ) of the calcination process was calculated as follows:

$$\eta_{ex-overall} = \frac{Ex_{ch,lm}}{Ex_{ew}} \quad (45)$$

in which  $Ex_{ew}$  is the exergy flow of eucalyptus wood consumed in the calcination process. The physical exergy part of the eucalyptus wood ( $Ex_{ph,ew}$ ) is negligible as it is at dead state temperature, and the fraction of chemical exergy of the eucalyptus wood ( $Ex_{ch,ew}$ ) was determined based on its chemical composition, specifically for dry biomass, in kW [33]:

$$Ex_{ch,ew} = \left( 1812.5 + 295.606C + 587.354H + 17.506O + 17.735N - 31.8A \right) \cdot m_{ew} \quad (46)$$

where  $C$ ,  $H$ ,  $O$ ,  $N$ , and  $A$  are the percentages of carbon,

hydrogen, oxygen, nitrogen, and ash, respectively, that constitute the eucalyptus wood.

The specific energy consumption of the limekiln ( $SEN$ ), which characterizes the amount of fuel energy consumed per ton of produced quicklime ( $m_{lm}$ ), was determined as follows [6]:

$$SEN = \frac{v_{pg} LHV_{pg}}{m_{lm}} \quad (47)$$

And the overall specific energy consumption ( $SEN_{overall}$ ) of the calcination process was assessed, taking into account the energy consumption from eucalyptus wood, in this way:

$$SEN_{overall} = \frac{m_{ew} LHV_{ew}}{m_{lm}} \quad (48)$$

## RESULTS AND DISCUSSIONS

In this chapter, the outcomes of mass, energy, and exergy balances obtained for the investigated limekiln's CV, referred to as "Kiln 1", which operates with producer gas as a renewable biofuel derived from eucalyptus wood gasification, are presented and discussed.

These results obtained for Kiln 1 were primarily compared with findings from two similar vertical annular shaft limekilns that operate using non-renewable fossil fuels. These two limekilns, designated as Kiln 2 and Kiln 3, were investigated by [16] and [34], respectively, and utilize oil and lignite dust as non-renewable fossil fuels. Moreover, other literature data for analogous vertical annular shaft limekilns were also compared with the Kiln 1 investigated herein, in which case the citations were provided accurately.

Literature data were presented as provided by the references, and with temperatures standardized in degrees Celsius. The operational data of limekilns of the same type vary even among literature data. This occurs due to, for example, differences in local temperature, control systems, chemical compositions of limestone, quicklime, and the fuel, and substance flow rates. Thus, the comparisons made in this work were generally made in specific terms and are similar to those made in the literature [6,16], and were not intended to affirm that one fuel is better than another in terms of energy or exergy. The comparisons were made in this work to verify that the methodology used is feasible and capable of providing operational data from a company using locally available sustainable biofuel as a substitute for traditional fossil fuels.

### Mass balance results

Table 2 shows the results of mass flows and by

percentage of constituent chemical species for Kiln 1. It can be seen that the sum of input mass flows in Kiln 1 ( $m_{in-cv}$ ) is equivalent to the sum of output mass flows ( $m_{out-cv}$ ), according to the mass conservation principle presented in Eq. (9).

From Table 2, it is noted that Kiln 1 operates with a proportion of 0.767 kg of CO<sub>2</sub> from calcination per kg of quicklime produced. This same parameter is commonly reported in the literature for the characterization of calcination processes, with typical values of 0.751 [35], 0.786 [6], and 0.783–0.786 [36] kg of CO<sub>2</sub> per kg of quicklime produced. These data are in accordance with the result achieved for Kiln 1.

Considering the total amount of CO<sub>2</sub> emitted, including the calcination and fuel combustion, Kiln 1 works with an emission ratio of 1.427 kg of CO<sub>2</sub> per kg of quicklime produced. This parameter is also traditionally reported in the literature as a specification of calcination processes. This result for the total quantity of CO<sub>2</sub> emitted per kg of quicklime produced attained in Kiln 1, is also in consonance with literature results with values of 1.092 [35], 1.113–1.129 [36], 1.221–1.401 [6] kg of CO<sub>2</sub> per kg of quicklime produced. These emission ratios were not reported for Kilns 2 and 3 by the literature.

As previously mentioned, note that limekiln specifications can vary from one literature source to another. This occurs, for example, due to differences in local temperatures, control systems, limekiln design, chemical compositions of the limestone, quicklime, and the fuel, and substances flow rates.

### Energy balance results

In Table 3, the results of energy flows and in terms of chemical species percentage for Kiln 1 were presented. As indicated in Eq. (24), it is noted that the sum of energy flows entering CV ( $En_{in-cv}$ ) is equivalent to the sum of energy flows leaving CV ( $En_{out-cv}$ ) plus the energy required for calcination ( $En_{cr}$ ), thus satisfying the energy conservation principle.

Note that of the total input energy flow provided by the producer gas, this is mostly distributed to the limestone calcination ( $En_{cr}$ ). This was expected because limestone calcination is an industrial process that requires a large amount of energy [16].

The exhaust gases, which include  $En_{pc}$  and  $En_{CO_2(g)-cr}$ , have a considerable energy content released into the atmosphere, and are therefore wasted. Hence, the heat from the exhaust gases of Kiln 1 could be recovered. This could be achieved with the implementation of a recirculation system directing the gases into the limekiln. Doing so would preheat the

Table 2. Kiln 1 mass balance results.

Mass flow (kg/h)	Input Chemical species mass (%)	Mass flow (kg/h)	Output Chemical species mass (%)
$m_{ls} = 4455.1$	$m_{CaCO_3(s)} = 0.9335 \cdot m_{ls}$ $m_{CaCO_3 \cdot MgCO_3(s)} = 0.0494 \cdot m_{ls}$ $m_{SiO_2(s)} = 0.0155 \cdot m_{ls}$ $m_{Al_2O_2(s)} = 0.0009 \cdot m_{ls}$ $m_{Fe_2O_2(s)} = 0.0007 \cdot m_{ls}$	$m_{pc} = 6112.5$	$m_{H_2O(g)} = 0.0607 \cdot m_{pc}$ $m_{CO_2(g)} = 0.2641 \cdot m_{pc}$ $m_{O_2(g)} = 0.0179 \cdot m_{pc}$ $m_{N_2(g)} = 0.6573 \cdot m_{pc}$
$m_a = 3604.8$	$m_{O_2(g)} = 0.2329 \cdot m_a$ $m_{N_2(g)} = 0.7671 \cdot m_a$	$m_{CO_2(g)-cr} = 1875.2$	-
$m_{pg} = 2507.6$	$m_{N_2(g)} = 0.4996 \cdot m_{pg}$ $m_{CO(g)} = 0.1399 \cdot m_{pg}$ $m_{H_2(g)} = 0.0065 \cdot m_{pg}$ $m_{CO_2(g)} = 0.3140 \cdot m_{pg}$ $m_{CH_4(g)} = 0.0401 \cdot m_{pg}$	$m_{sw} = 1.5$	$m_{CaCO_3(s)} = 0.0717 \cdot m_{sw}$ $m_{CaCO_3 \cdot MgCO_3(s)} = 0.5645 \cdot m_{sw}$ $m_{SiO_2(s)} = 0.1581 \cdot m_{sw}$ $m_{Al_2O_2(s)} = 0.1457 \cdot m_{sw}$ $m_{Fe_2O_2(s)} = 0.0599 \cdot m_{sw}$ $m_{CaO(s)} = 0.9510 \cdot m_{tm}$ $m_{MgO(s)} = 0.0190 \cdot m_{tm}$ $m_{SiO_2(s)} = 0.0273 \cdot m_{tm}$ $m_{Al_2O_2(s)} = 0.0015 \cdot m_{tm}$ $m_{Fe_2O_2(s)} = 0.0012 \cdot m_{tm}$
		$m_{tm} = 2444.7$	$m_{CaCO_3(s)} = 0.9335 \cdot m_{ls-ub}$ $m_{CaCO_3 \cdot MgCO_3(s)} = 0.0494 \cdot m_{ls-ub}$ $m_{SiO_2(s)} = 0.0155 \cdot m_{ls-ub}$ $m_{Al_2O_2(s)} = 0.0009 \cdot m_{ls-ub}$ $m_{Fe_2O_2(s)} = 0.0007 \cdot m_{ls-ub}$
		$m_{ls-ub} = 133.7$	
$m_{in-cv} = 10567.5$		$m_{out-cv} = 10567.5$	

Table 3. Kiln 1 energy balance results.

Energy flow (kW)	Input Chemical species energy (%)	Energy flow (kW)	Output Chemical species energy (%)
$En_{ls} = 0$	$En_{CaCO_3(s)} = 0$ $En_{CaCO_3 \cdot MgCO_3(s)} = 0$ $En_{SiO_2(s)} = 0$ $En_{Fe_2O_2(s)} = 0$ $En_{Al_2O_2(s)} = 0$	$En_{pc} = 315.8$	$En_{H_2O(g)} = 0.1073 \cdot En_{pc}$ $En_{CO_2(g)} = 0.2340 \cdot En_{pc}$ $En_{O_2(g)} = 0.0159 \cdot En_{pc}$ $En_{N_2(g)} = 0.6427 \cdot En_{pc}$
$En_a = 0$	$En_{O_2(g)} = 0$ $En_{N_2(g)} = 0$	$En_{CO_2(g)-cr} = 85.8$	-
$En_{pg} = 3227.1$	$En_{N_2(g)} = 0.0415 \cdot En_{pg}$ $En_{CO(g)} = 0.3168 \cdot En_{pg}$ $En_{H_2(g)} = 0.1752 \cdot En_{pg}$ $En_{CO_2(g)} = 0.0249 \cdot En_{pg}$ $En_{CH_4(g)} = 0.4415 \cdot En_{pg}$	$En_{sw} = 0.1$	$En_{CaCO_3(s)} = 0.0662 \cdot En_{sw}$ $En_{CaCO_3 \cdot MgCO_3(s)} = 0.6265 \cdot En_{sw}$ $En_{SiO_2(s)} = 0.1332 \cdot En_{sw}$ $En_{Al_2O_2(s)} = 0.1310 \cdot En_{sw}$ $En_{Fe_2O_2(s)} = 0.0431 \cdot En_{sw}$ $En_{CaO(s)} = 0.9468 \cdot En_{tm}$ $En_{MgO(s)} = 0.0234 \cdot En_{tm}$ $En_{SiO_2(s)} = 0.0272 \cdot En_{tm}$ $En_{Al_2O_2(s)} = 0.0016 \cdot En_{tm}$ $En_{Fe_2O_2(s)} = 0.0010 \cdot En_{tm}$
		$En_{tm} = 18.4$	$En_{CaCO_3(s)} = 0.9209 \cdot En_{ls-ub}$ $En_{CaCO_3 \cdot MgCO_3(s)} = 0.0639 \cdot En_{ls-ub}$ $En_{SiO_2(s)} = 0.0138 \cdot En_{ls-ub}$ $En_{Al_2O_2(s)} = 0.0008 \cdot En_{ls-ub}$ $En_{Fe_2O_2(s)} = 0.0005 \cdot En_{ls-ub}$
		$En_{ls-ub} = 1.1$	
		$En_{wt} = 645.4$	
		$En_{cr} = 2160.5^*$	$\Delta H_{R-CaCO_3(s)}^\circ = 0.9535 \cdot En_{cr}$ $\Delta H_{R-CaCO_3 \cdot MgCO_3(s)}^\circ = 0.0465 \cdot En_{cr}$
$En_{in-cv} = 3227.1$		$En_{out-cv} + En_{cr} = 3227.1$	

limestone entering the equipment at ambient temperature, contributing to its calcination. Consequently, this could reduce the consumption of producer gas. This gas recirculation technology is commonly used in the lime sector [15], however the visited company lacks this equipment.

In Fig. 3, a Sankey diagram comparison of energy flow results for Kilns 1, 2, and 3 was made. It is perceived that the limestone and combustion air energy input flows in Kiln 1 were considered insignificant, as both flows are at ambient temperature. Similarly, in Kilns 2 and 3 the limestone and combustion air input energies represent insignificant fractions, with a maximum of 1.1% for combustion air energy in Kiln 3.

The fuel energy flow corresponds to the majority fraction of the sum of energies entering the three limekilns. In Kiln 1, the producer gas energy corresponds to 100%, being, therefore, in accordance with the fossil fuels percentages, oil, and lignite dust, used in Kilns 2 and 3, respectively, 98.2 and 98.4%.

Regarding the output flows, the energy of exhaust gases is 12.4% of the sum of input energies in Kiln 1, while for Kilns 2 and 3 it is equivalent to 29.3% and 23.2%, respectively. It can be noted that the higher the output temperature of the exhaust gases, the greater the energy wasted in this flow. This is evidenced because the Kiln 2 operates with the highest output temperature (455.0 °C) and fraction of exhaust gases energy (29.3%), while the Kiln 1 investigated herein works with the lowest values of these parameters, 198.2 °C and 12.4%, respectively.

In Kiln 1, the quicklime energy corresponds to 0.6%, being similar to 0.6% in Kiln 3, while in Kiln 2 it represents 4.8%. It is observed that in Kiln 2, the quicklime leaves the equipment at a considerably higher temperature (277.0 °C) compared to Kilns 1 (60.0 °C) and 3 (35.0 °C), which results in a significant waste of 4.8% of the energy supplied.

The wall loss energy corresponds to 20.0% in Kiln 1, being higher than in Kiln 2 (9.1%) and Kiln 3 (4.6%). In Kiln 1, the solid waste and unburnt limestone energies have the lowest energy fractions, being 0.002% and 0.03%, respectively. These two results are also consistent with Kilns 2 and 3, as they were disregarded.

As in Kiln 1, in Kilns 2 and 3 the energy content of the exhaust gases could be recovered through the gas recirculation system mentioned in this section. The heat recovered from the exhaust gases can contribute to limestone calcination and reduce fuel consumption and manufacturing cost. In this way, according to Eq. (42), the energy efficiency ( $\eta_{en}$ ) can be increased. Another

option to further improve the energy efficiency of the limekilns would be to apply an operational control method to find optimal operational values of variables such as the exhaust gas and quicklime output temperatures. This type of operational control method was also employed by [32] for operational variables of a vertical industrial limekiln, achieving reductions in fuel and raw material consumption and environmental impacts, in addition to improving the quality of the quicklime.

In the Sankey diagrams shown in Fig. 3, it can be seen that the energy required for calcination corresponds to the largest portion of the total input energy, being 66.9% in Kiln 1, similar to Kiln 3 with 71.6%, while in Kiln 2 it was 56.8%. The suitability of the methodology applied in this work can be perceived through the consistency of the results achieved for Kiln 1 investigated herein with those of Kilns 2 and 3 in the literature.

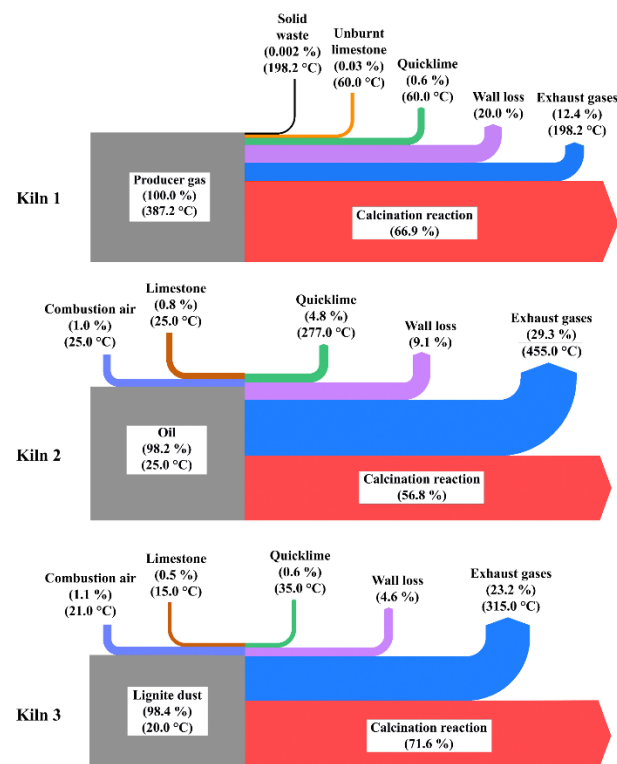


Figure 3. Energy Sankey diagrams for the kilns.

## Exergy balance results

Table 4 shows the results achieved for exergy flows of the CV of Kiln 1, and the contributions of physical and chemical exergies in each flow. The temperatures and percentages of the exergy of each flow were also presented in relation to the total exergy entering the equipment. It can be seen that Eq. (34) is being satisfied because the sum of exergy flows entering CV ( $Ex_{in-CV}$ ) corresponds to the sum of exergy flows leaving it ( $Ex_{out-CV}$ ) plus the destroyed

Table 4. Kiln 1 exergy balance results.

Input						Output					
Flow	T (°C)	Ex <sub>ph</sub> (kW)	Ex <sub>ch</sub> (kW)	Ex (kW)	% <sub>total</sub>	Flow	T (°C)	Ex <sub>ph</sub> (kW)	Ex <sub>ch</sub> (kW)	Ex (kW)	% <sub>total</sub>
$Ex_{ls}$	25.0	0	19.4	19.4	0.6	$Ex_{tm}$	60.0	1.0	1293.2	1294.2	42.0
$Ex_a$	25.0	0	0	0	0	$Ex_{eg}$	198.2	86.1	363.5	449.6	14.6
$Ex_{pg}$	387.2	107.2	2957.1	3064.3	99.4	$Ex_{wl}$	-	-	-	220.2	7.1
						$Ex_{sw}$	198.2	0.02	0.15	0.17	0.01
						$Ex_{ls-ub}$	60.0	0.1	0.6	0.7	0.02
						$Ex_D^a$				1118.9	36.3
$Ex_{in-cv}$	-	107.2	2976.6	3083.8	100.0	$Ex_{out-cv} + Ex_D$		87.2	1657.4	3083.8	100.0

exergy flow ( $Ex_D$ ).

Fig. 4 shows a Sankey Diagram comparison of the results of exergy flows obtained in Kilns 1, 2, and 3. The temperature and percentages of physical and chemical exergies in each flow were also presented. Eq. (34) is being satisfied in all limekilns, where the exergies that enter these, are equivalent to the exergies that leave plus the destroyed exergy.

Analyzing Table 4 and Fig. 4, it is noted that the highest physical exergy content, which is recoverable, is related to the exhaust gas output flow in the three limekilns. The amount of physical exergy of quicklime is low compared to its chemical exergy in the three kilns. This reinforces the importance of implementing a gas recirculation system and the application of the operational control method for optimal values of variables, such as the exhaust gas output temperature. The recovery of physical exergy from exhaust gases and quicklime can support limestone calcination and reduce fuel consumption, and according to Eq. (44), increase the exergy efficiency ( $\eta_{ex}$ ) of limekilns.

As shown in Fig. 4, the limestone exergy flow has no physical exergy fraction in all kilns, as this flow is at dead state temperature. Therefore, the limestone chemical exergy portion corresponds to its total exergy, being 0.6%, 5.6%, and 6.1% of the sum of input exergies, in Kilns 1, 2, and 3, respectively.

The combustion air exergy represents the smallest contribution of the sum of input exergies in all limekilns. In Kiln 1, the physical and chemical exergies of combustion air were disregarded because the air is atmospheric under dead state conditions. Similarly, the combustion air physical exergy is negligible in Kiln 3 and zero in Kiln 2. In Kilns 2 and 3, combustion air exergies have contributions of 1.7% and 3.3%, respectively.

The fuel exergy flow corresponds to the largest contribution of the sum of input exergies in all limekilns. In Kiln 1, the producer gas exergy, the renewable biofuel, has a contribution of 99.4%, comprised mostly of 96.5% of chemical exergy. Similarly, the fossil fuel exergies in Kilns 2 and 3 are equivalent to 92.7% and 90.6%, respectively, being composed solely of

chemical exergy.

As seen in Fig. 4, for output flows, the quicklime exergy is mainly comprised of chemical exergy and has contributions of 42.0%, 38.1%, and 41.0% in Kilns 1, 2, and 3, respectively, in relation to total input exergy.

The exhaust gas exergies correspond to similar percentages of 14.6%, 14.3%, and 11.2% in Kilns 1, 2, and 3 respectively. In Kilns 2 and 3, the exhaust gas exergies have contributions of 45.6% and 45.9% of chemical exergy, respectively, and 54.4% and 54.1% of physical exergy, respectively. Conversely, the exhaust gas exergy in Kiln 1 has a 19.1% contribution of physical exergy and 80.9% of chemical exergy. Kiln 1 operates with exhaust gases at considerably a lower temperature (198.2 °C) compared to Kiln 2 (455.0 °C) and 3 (315.0 °C), so, understandably, Kiln 1 has a lower contribution of physical exergy.

The wall loss exergies have similar percentages of 7.1%<sup>></sup>, and 1.3% in Kilns 1, 2, and 3, respectively. The unburnt limestone and solid waste exergies in Kiln 1 have insignificant contributions of 0.02% and 0.01%, respectively, and in Kilns 2 and 3 they were disregarded.

Through the exergy balance expressed in Eq. (34), the sum of output exergies from Kilns 1, 2, and 3 has similar percentages of respectively 63.7%, 58.5%, and 53.5% of the sum of input exergies. Consequently, the destroyed exergy corresponds to the remaining fraction of total input exergy, being 36.3%, 41.5% and 46.5% in Kilns 1, 2, and 3, respectively. The destroyed exergy is inherent to the characteristic irreversibilities of real thermodynamic processes according to the second law of thermodynamics. Examples of sources of irreversibilities in limekilns are the chemical reactions of combustion and calcination, and heat transfer processes in the equipment [16]. As can be seen, the destroyed exergy in Kiln 1 investigated herein was 5.2% and 10.2% lower than in Kilns 2 and 3 of the literature, respectively.

In Fig. 4, it is perceived that the total input exergy in Kiln 1 is distributed in the following descending order: quicklime exergy (42.0%), destroyed exergy (36.3%), exhaust gases (14.6%), wall loss (7.1%), unburnt

limestone (0.02%) and solid waste (0.01%). Similarly, it can be seen that in Kilns 2 and 3 the total input exergy was mostly distributed in destroyed exergy, which is followed by quicklime, exhaust gases, and wall loss exergies, these three in the same decreasing order obtained in Kiln 1. The correspondence of the results attained for Kiln 1 with Kilns 2 and 3 in the literature, indicates the suitability of the applied analysis methodology for scrutinizing the limekilns.

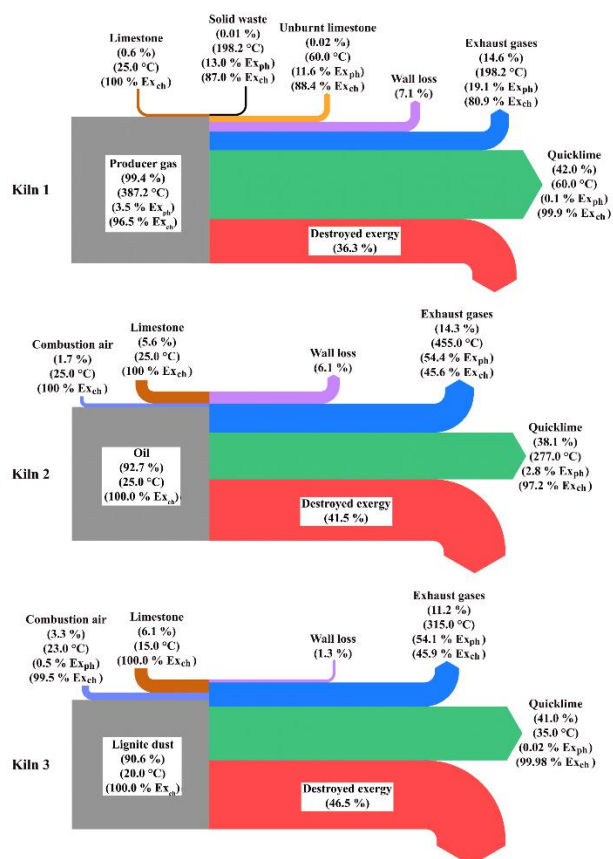


Figure 4. Exergy Sankey diagrams for the kilns.

## Efficiencies and *SEN* results

This section presents the results achieved in the present work and also some found in the literature for similar vertical limekilns. The specific energy (*SEN*) found in the present study for the Kiln 1 was 4.8 GJ of producer gas energy consumed per ton of quicklime produced, in agreement with the literature *SEN* values of 4.0–4.8 [15], 4.4 [34], 4.7 [16], and 5.45–5.82 GJ/t [6]. The *SEN* value of Kiln 1 is in agreement with those of Kilns 2 (4.7 GJ/t) and 3 (4.4 GJ/t), studied by [16] and [34] respectively.

And considering the overall calcination process, the overall specific energy ( $SEN_{overall}$ ) achieved was 7.6 GJ of eucalyptus wood energy consumed per ton of quicklime produced, which is higher than the literature *SEN* values aforementioned. According to Eqs. (47) and (48), lower *SEN* values are desirable, as less fuel

energy is consumed to produce quicklime.

Considering the producer gas energy consumption, the energy efficiency ( $\eta_{en}$ ) evaluated with Eq. (42) for Kiln 1 was 54.6%, which complies with the  $\eta_{en}$  found for similar limekilns operating with fossil fuels studied in the literature, with values of: 54.68–58.33 [6], 57.8 (Kiln 2) [16], 72.8 (Kiln 3) [34], and 65–77% [15].

Considering the eucalyptus wood energy consumption, the overall energy efficiency ( $\eta_{en-overall}$ ) assessed with Eq. (43) was 42.0%, which is lower than the  $\eta_{en}$  aforementioned by the literature.

When considering the exergy consumption of producer gas, the exergy efficiency ( $\eta_{ex}$ ) determined using Eq. (44) for Kiln 1 was 42.2%. This value aligns with  $\eta_{ex}$  values reported in the literature for similar limekilns performing with fossil fuels, such as 40.0 [7], 40.0 (Kiln 2) [16], and 45.3% (Kiln 3) [34].

And considering the eucalyptus wood exergy consumption, the overall exergy efficiency ( $\eta_{ex-overall}$ ), calculated using Eq. (45), was 23.6%, being lower than the  $\eta_{ex}$  mentioned in the literature cited previously.

The efficiency of Kiln 1 using producer gas as a biofuel does not present an advantage compared to the efficiency of limekilns employing traditional fossil fuels. However, the authors emphasize that it was possible to propose a diagnostic of a calcination process of a company where an environmentally friendly biofuel is used with efficiencies close to those of limekilns employing conventional fossil fuels. Additionally, the company reported that the use of sustainable biofuel in its calcination process is due to its low cost compared to fossil fuels, environmental friendliness, and compliance with atmospheric emission limits without impacting the quality of quicklime. The company could not provide us with information regarding the cost of the renewable biofuel used.

In summary, as detailed previously, to enhance the values of *SEN*, energy efficiency, and exergy efficiency of Kiln 1, which operates with producer gas derived from eucalyptus wood gasification, as well as of other limekilns using fossil fuels, it is essential to emphasize the significance of recovering energy and exergy from exhaust gases and heat wall loss of the equipment. This can be achieved through the implementation of a gas recirculation system, a technique already employed in the quicklime industry. Furthermore, by employing operational control methods for limekiln variables, parameters such as exhaust gas and quicklime output temperatures can be adjusted to optimal values, further enhancing energy and exergy efficiencies, as well as *SEN* of the limekilns. Additionally, the kinetic energy of the exhaust gases

could be converted into electric energy through the implementation of a turbine-generator system. Thus, this electric energy could be utilized to power the electric equipment of the calcination process, including panels and air blowers.

## CONCLUSION

This work conducts energy and exergy diagnostics of a vertical industrial limekiln, which uses producer gas as renewable biofuel produced from eucalyptus wood gasification. Industrial data, coupled with some literature data for equipment characterization, were utilized in these diagnostics. The obtained results were compared with those from similar limekilns using fossil fuels. The Specific Energy Consumption ( $SEN$ ) for the producer gas-operated limekiln was 4.8 GJ/t<sub>quicklime</sub>, along with energy ( $\eta_{en}$ ) and exergy ( $\eta_{ex}$ ) efficiencies of 54.6% and 42.2%, respectively. These results align with those found in the literature for analogous limekilns utilizing fossil fuels. In overall terms, the overall energy ( $\eta_{en-overall}$ ) and exergy ( $\eta_{ex-overall}$ ) efficiencies were 42.0% and 23.6% respectively, being lower than literature values. The  $SEN_{overall}$  (7.6 GJ/t<sub>quicklime</sub>) was higher than the literature results. To enhance the performance of both renewable biofuel-operated and fossil fuel-operated limekilns, potential areas for energy and exergy recovery were identified. These include mainly recovering heat from exhaust gases, reducing thermal losses through limekiln walls, and deploying operational control methods to adjust variables such as exhaust gas and quicklime temperatures. These findings provide valuable insights for researchers exploring the adoption of renewable biofuels like eucalyptus wood-derived producer gas as alternatives to conventional fossil fuels in limekilns.

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NAUČNI RAD

## ENERGETSKA I EKSERGETSKA DIJAGNOSTIKA INDUSTRIJSKE ŠAHTNE PEĆI ZA PEČENJE KREČA NA PROIZVODNI GAS KAO OBNOVLJIVIM BIOGORIVOM

*Živi kreč, globalno značajna roba koja se koristi u različitim industrijskim aplikacijama, proizvodi se u krečnim pećima koje zahtevaju značajnu energiju, tradicionalno, iz fosilnih goriva. Međutim, zbog rastućih ograničenja emisija i iscrpljivanja naslaga fosilnih goriva, industrija živog kreča istražuje alternativna goriva, kao što je biomasa. U literaturi nedostaju dijagnostičke studije izvodljivosti za krečne peći koje koriste alternativna goriva iz biomase. Stoga, ovaj rad ima za cilj da sprovede energetsku i eksergijsku dijagnostiku industrijske krečne peći koje koristi proizvodni gas dobijen iz drveta eukaliptusa kao obnovljivo biogorivo. Koristeći industrijske podatke i principe termodinamike, korišćena oprema je okarakterisana, a rezultati su upoređeni sa literaturnim nalazima za slične krečne peći koje koriste fosilna goriva. Specifična potrošnja energije za krečnu peć na proizvodni gas je bila 4,8 GJ/t kreča, sa energetskom i eksergijskom efikasnošću od 54,6% i 42,2%. Ukupna energetska i eksergijska efikasnost su bile za 42,0% i 23,6%, redom, niže od literaturnih vrednosti. Ukupna specifična potrošnja energije je bila 7,6 GJ/t kreča i većaše literaturnih vrednosti. Identifikovana poboljšanja za krečne peći na obnovljiva i fosilna goriva uključuju povraćaj energije i eksergija, uključujući povraćaj toplote iz izduvnih gasova, minimiziranje toplotnih gubitaka i optimizaciju operativnih varijabli. Ovi nalazi nude dragocene uvide za istraživače koji istražuju usvajanje obnovljivih biogoriva, kao što je proizvodni gas dobijen iz drveta eukaliptusa, kao alternativa konvencionalnim fosilnim gorivima u krečnim pećima.*

*Ključne reči: energija, eksergija, krečna peć, živi kreč, biomasa, biogorivo.*